

# CSCI 210: Computer Architecture

## Lecture 16: Combinational Logic

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Slides from Cynthia Taylor

# CS History: The Traitorous Eight



From left to right: Gordon Moore, C. Sheldon Roberts, Eugene Kleiner, Robert Noyce, Victor Grinich, Julius Blank, Jean Hoerni and Jay Last.  
Photo by Wayne Miller.

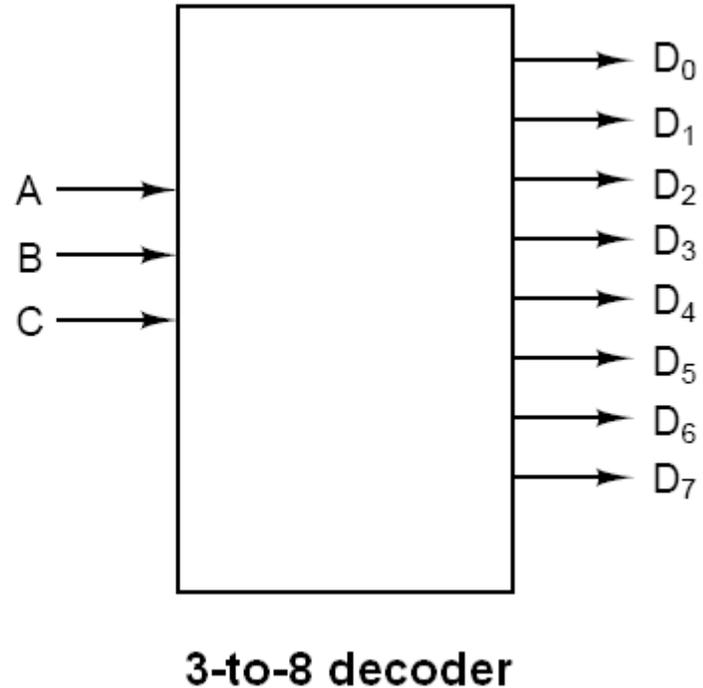
- All worked for William Shockley, inventor of the transistor, at Shockley Semiconductor
- Shockley was paranoid and a terrible manager
- In 1957, the “Traitorous Eight” left to form Fairchild Semiconductor
- All were between 26 and 33 years old when they left
- Fairchild Semiconductor became the leader of the industry, and was involved in the creation of many other companies, including Intel and AMD

# Digital Logic

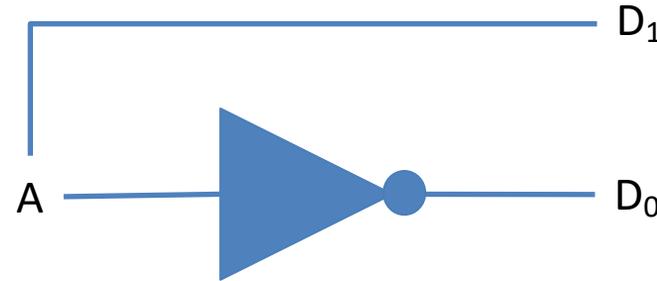
- Previously: Established rules of Boolean algebra and digital logic
- Today: Building stuff!

# Decoder

- Interprets  $n$  inputs (e.g., A, B, C) as an  $n$ -bit binary number
- Sets output  $D_n$  to 1, all other outputs to 0
- The output is “one hot”



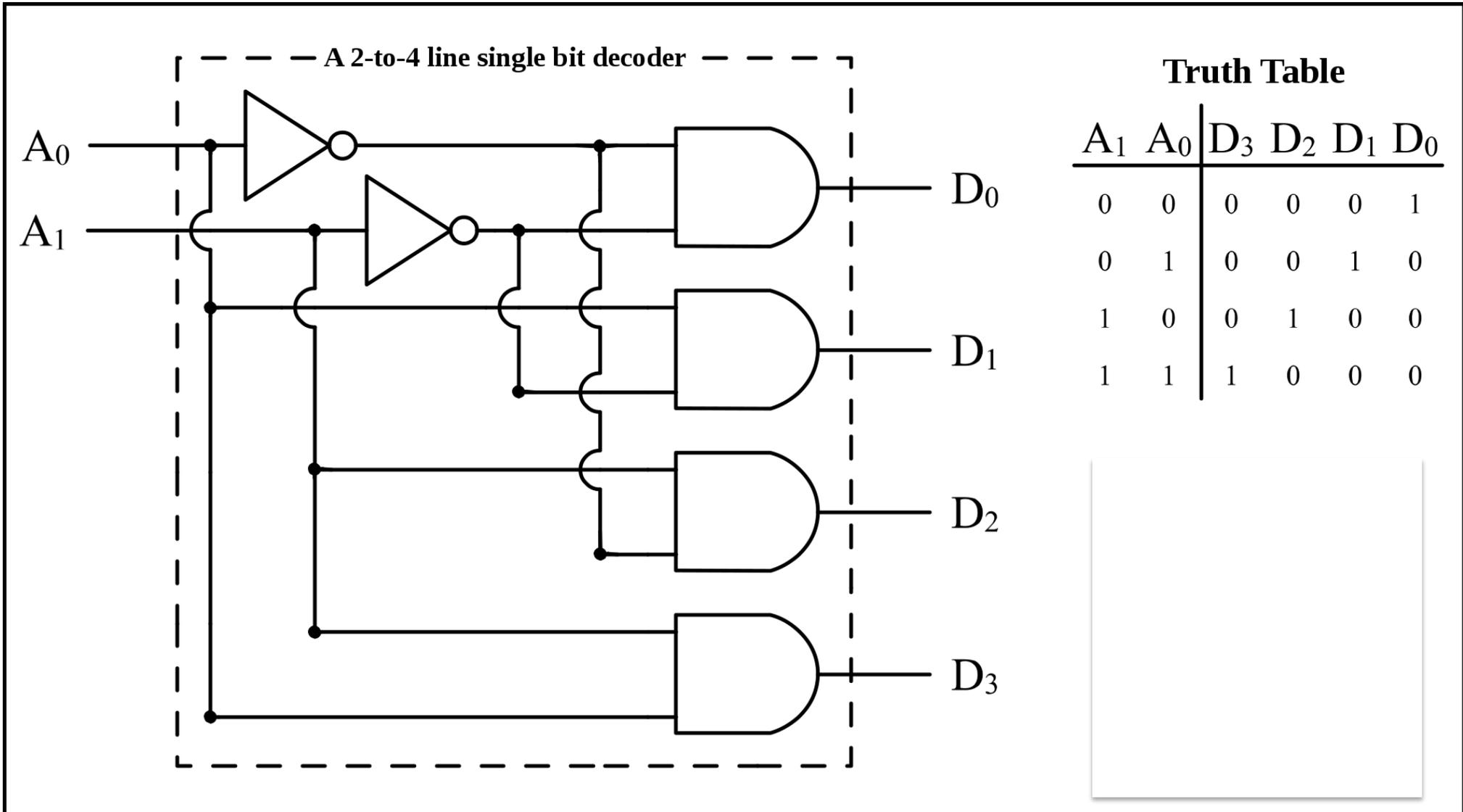
# Creating a Decoder



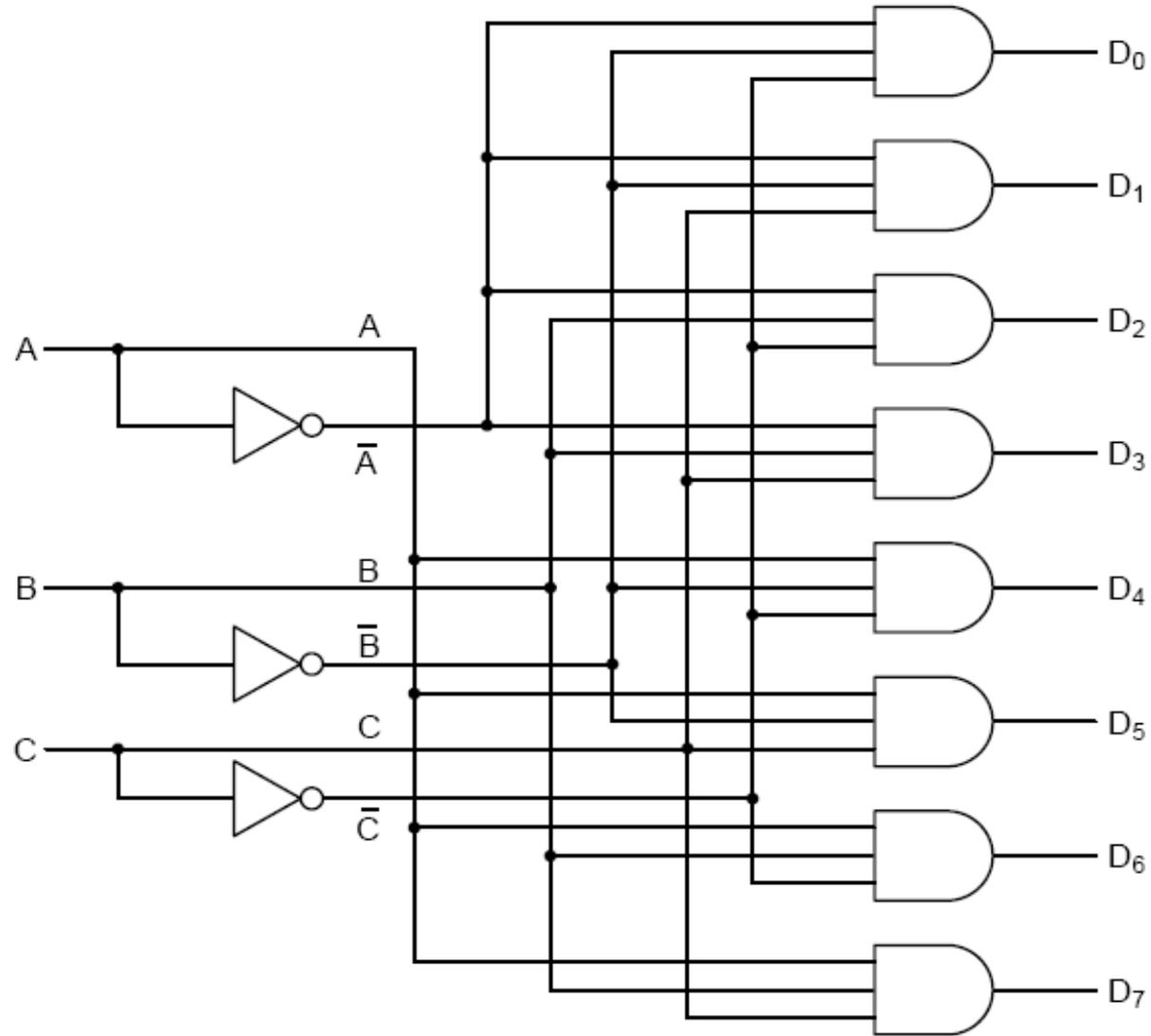
- For each input signal, we need the signal and its complement
- Signals are connected to outputs via AND gates so that inputs turn on only the output that the input represents (e.g., an input value of  $5 = 101_2$  turns on output  $D_5$ )

# 2-to-4 Decoder

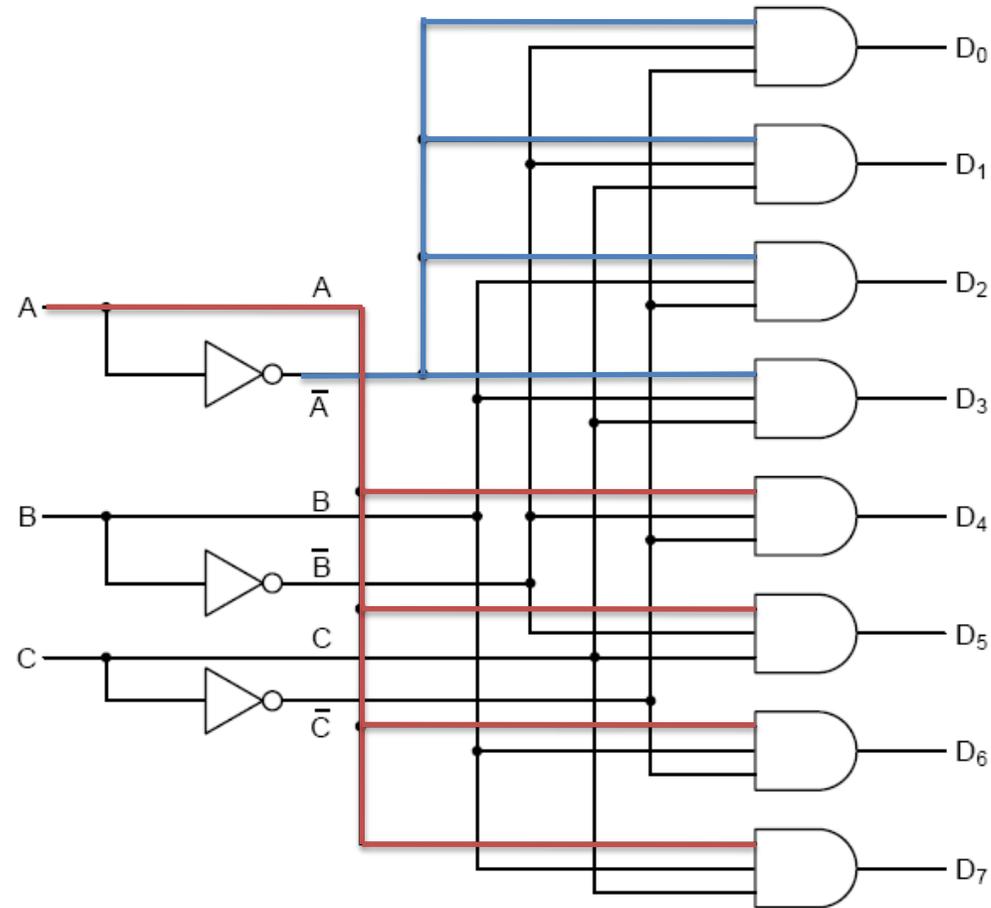
# 2-to-4 Decoder



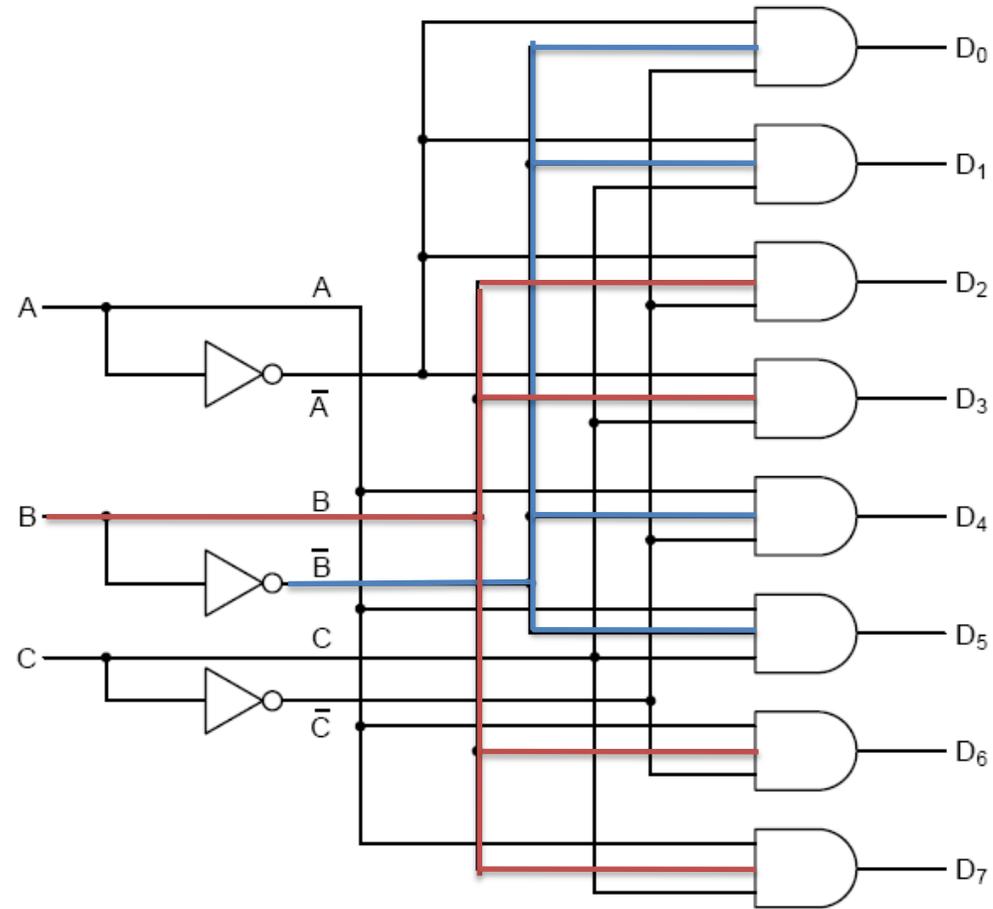
# 3-to-8 Decoder



# 3-to-8 Decoder, A is our MSB

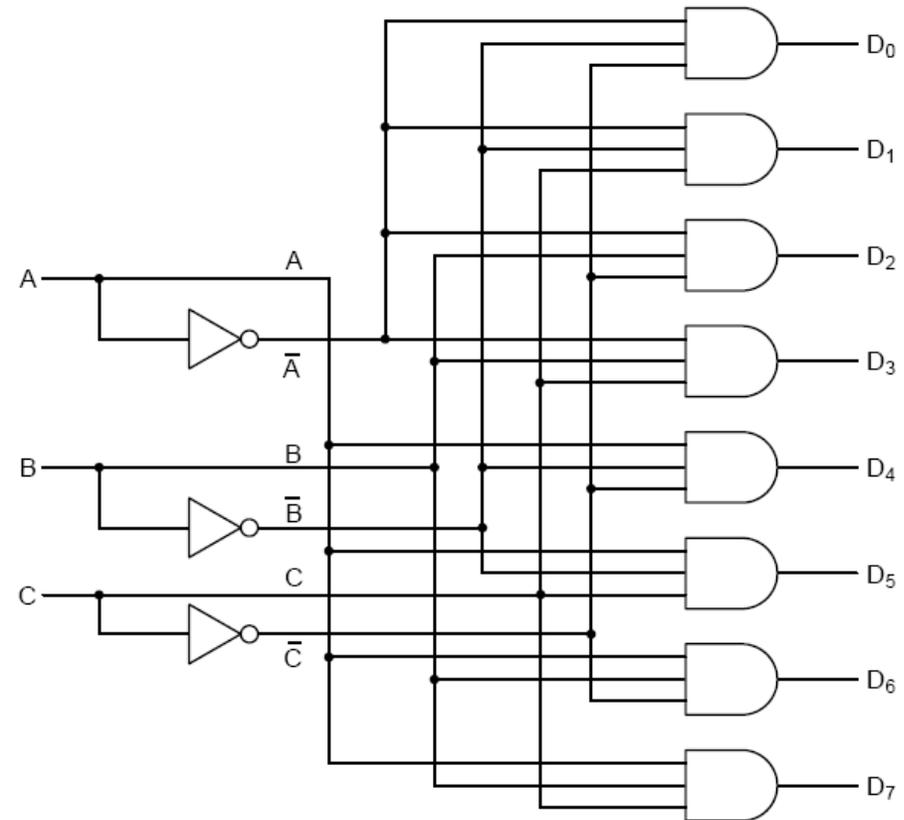


# 3-to-8 Decoder, B

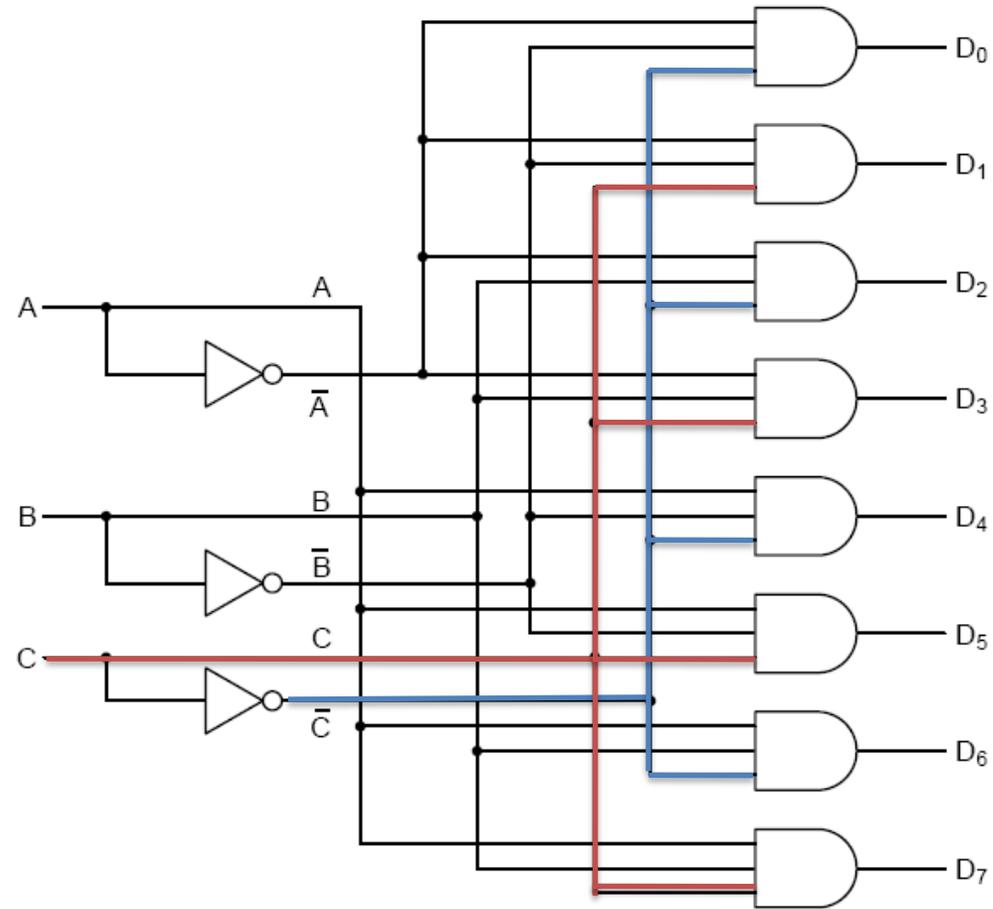


C corresponds to the lowest order bit for the input. In our 3-bit decoder, if C is 1, it sends 0 to \_ and 1 to \_

Clicker	0	1
A	D0, D1, D2, D3	D4, D5, D6, D7
B	D4, D5, D6, D7	D0, D1, D2, D3
C	D0, D2, D4, D6	D1, D3, D5, D7
D	D1, D3, D5, D7	D0, D2, D4, D6

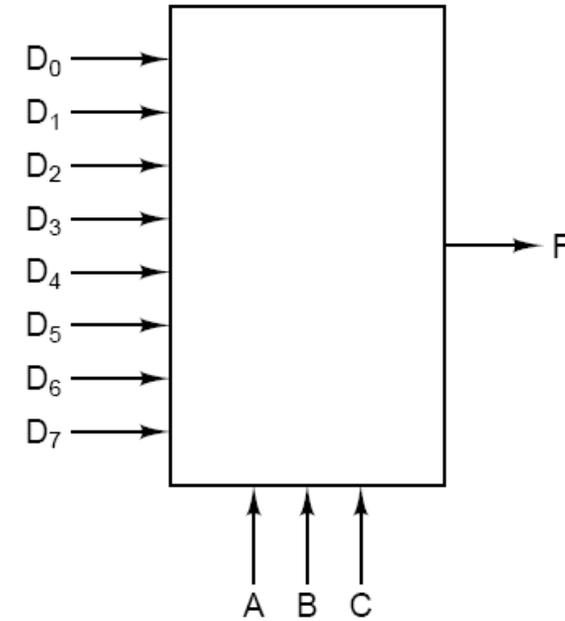


# 3-8 Decoder, C



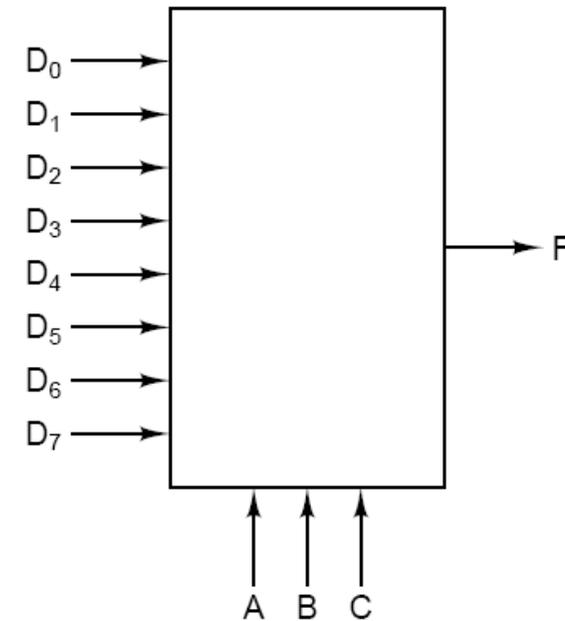
# Multiplexer

- Select one signal from a group of  $2^n$  inputs, to be output on a single output line.



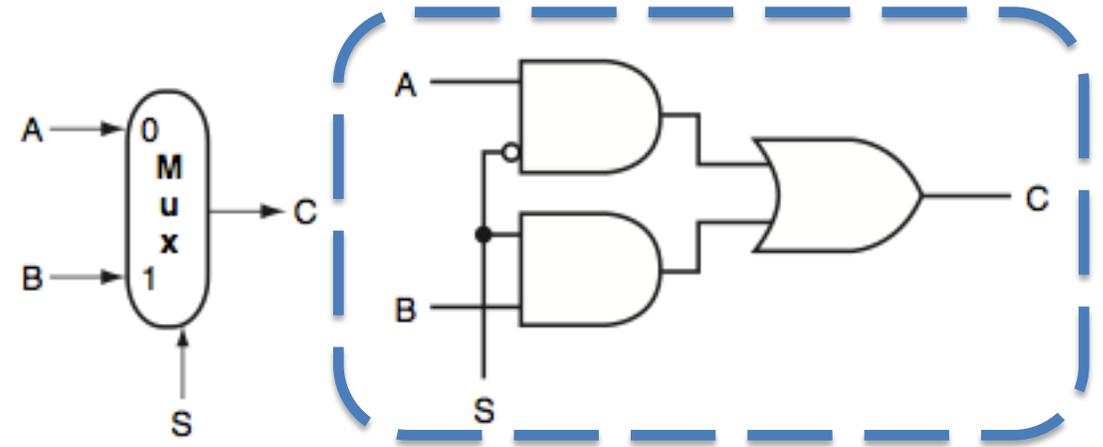
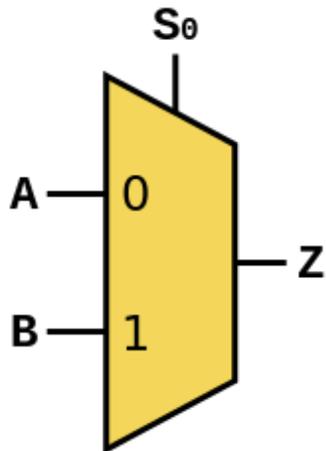
# Multiplexer

- Lines  $D_0, \dots, D_7$  are the data input lines and  $F$  is the output line.
- Lines  $A$ ,  $B$ , and  $C$  are called the select lines. They are interpreted as a three-bit binary number, which is used to choose one of the  $D$  lines to be output on line  $F$ .



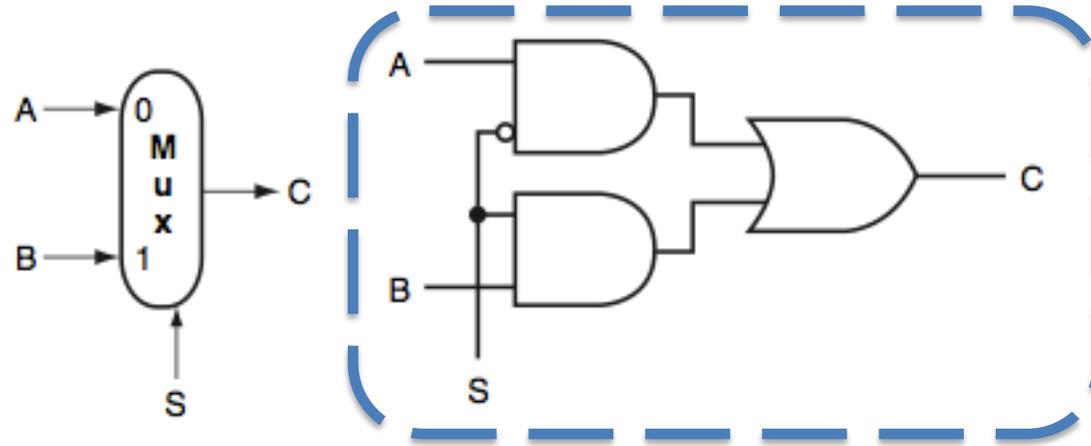
# 2-to-1 Multiplexer

- S is the selector
- S=0 selects A; S=1 selects B
- Common circuit symbol



Implementation

If  $A = 1$ ,  $B = 0$ , and  $S = 1$ , then  $C$  will be

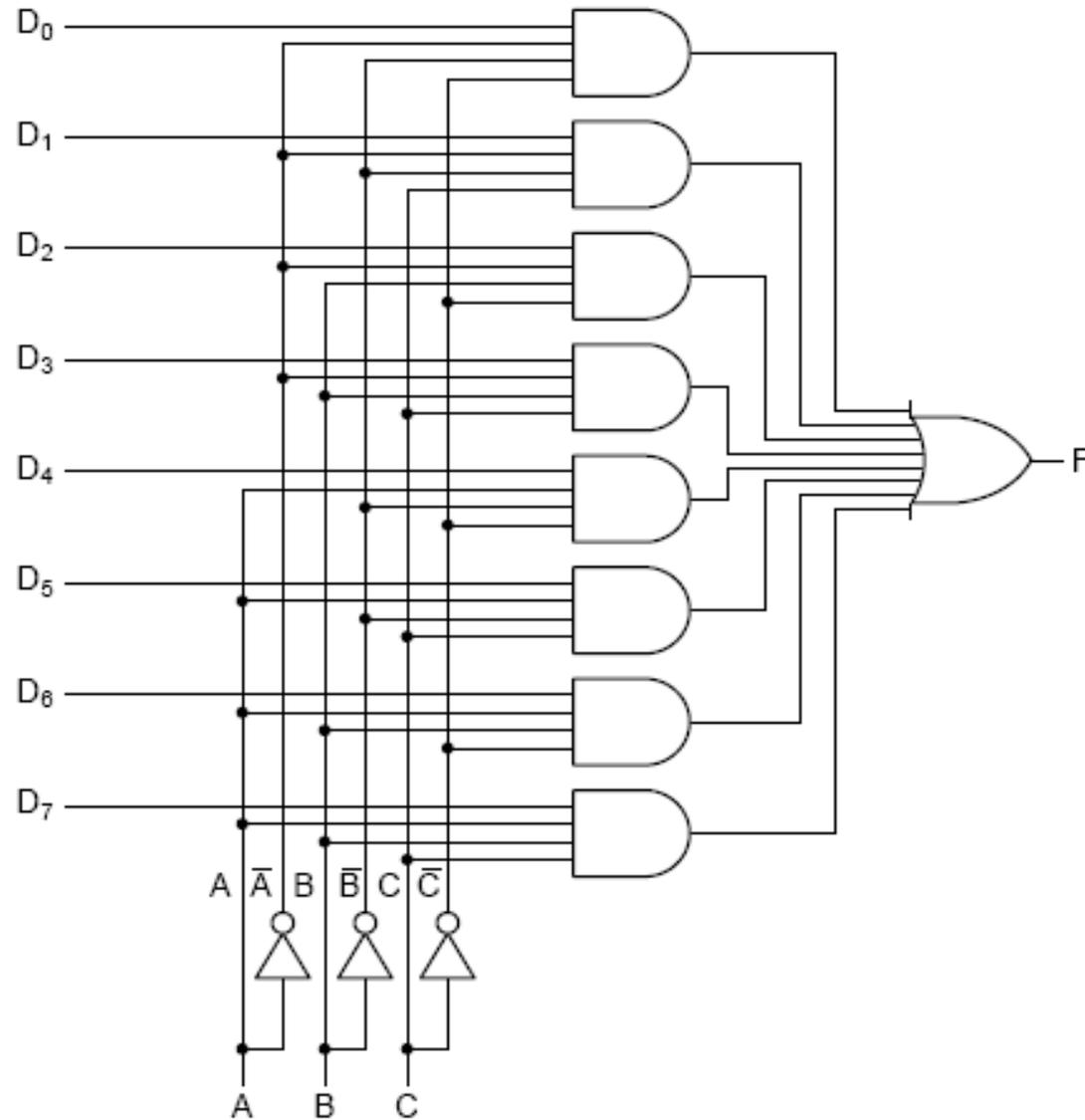


- A. 1
- B. 0
- C. Unclear

# Arbitrarily Large Multiplexer

- If there are  $n$  data inputs, there will need to be  $\lceil \log_2 n \rceil$  selector inputs.
- The multiplexer consists of
  - A decoder that generates  $n$  signals, each indicating a different control value
  - An array of  $n$  AND gates, each combining one of the inputs with a signal from the decoder
  - A single large OR gate that incorporates the outputs of the AND gates

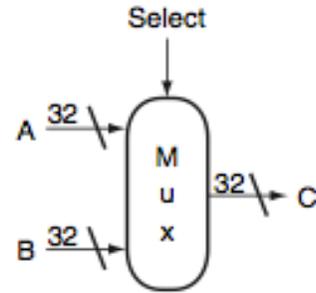
# 8-to-1 multiplexer



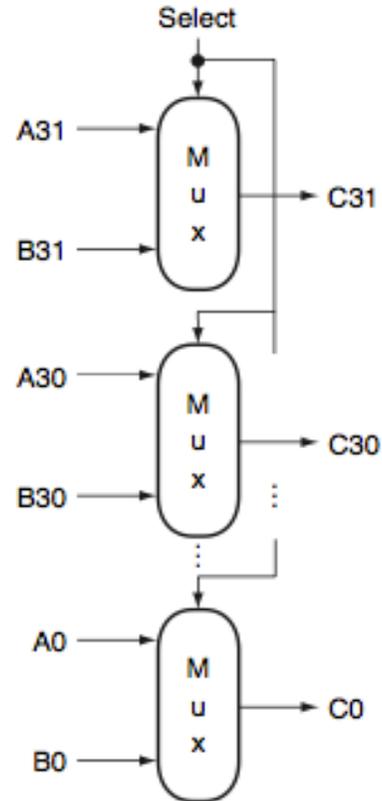
# Scaling Up

- Have to perform combinational operations over an entire word (32-bits) of input.
- Bus: a collection of data lines that is treated together as a single logical signal.
- Example: A multiplexer is used to choose which of the two buses (each 32 bits wide) will be written into the Result register

# Replicating a 1-bit Multiplexer 32 times



a. A 32-bit wide 2-to-1 multiplexer

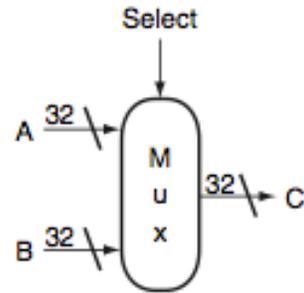


b. The 32-bit wide multiplexer is actually an array of 32 1-bit multiplexers

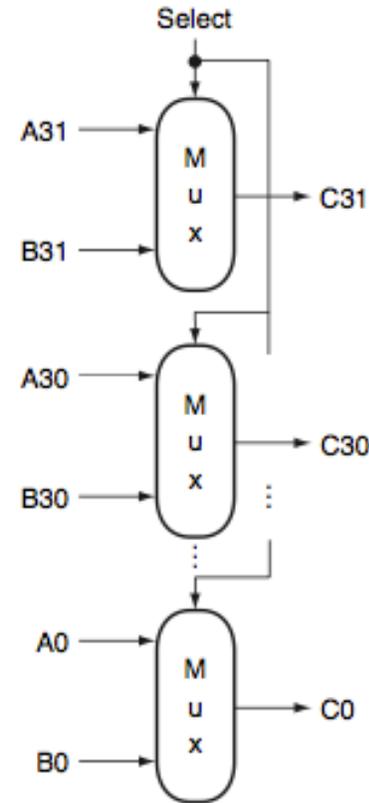
# Will the Select value be the same for each mux?

A. Yes

B. No



a. A 32-bit wide 2-to-1 multiplexer



b. The 32-bit wide multiplexer is actually an array of 32 1-bit multiplexers